National Institute of Open Schooling (NIOS) Senior Secondary Course Lesson –25:

Worksheet - Limits and Continuity

- 1. Limit of a function is approaches to a value. Justify with an example.
- **2.** Evaluate $\lim_{x\to 0} f(x)$ and $\lim_{x\to 1} f(x)$,

Where
$$f(x) = \begin{cases} 2x+3, & x \le 0 \\ 3(x+1), & x > 0 \end{cases}$$

- Find $\lim_{x \to 0} f(x)$, where $f(x) = \begin{cases} \frac{x}{|x|}, & x \neq 0 \\ 0, & x = 0 \end{cases}$
- **4.** When x = 5, evaluate

$$\lim_{x \to 5} \frac{3 - \sqrt{5 + x}}{5 - \sqrt{5 - x}}$$

- **5.** Differentiate between the value of a function at a point and the limit at a point with an example.
- **6.** If 'f' is an even function, then prove that $\lim_{x\to 0^-} f(x) = \lim_{x\to 0^+} f(x)$
- 7. Evaluate $\lim_{x \to 0} \frac{e^{7x} 1}{x}$
- 8. If $\lim_{x\to 2} \frac{x^n 2^n}{x 2} = 80$ and $n \in \mathbb{N}$, then find the value of n.

9. Examine the continuity of

$$f(x) = \begin{cases} \frac{|x-a|}{x-a}, & x \neq a \text{ at } x = a\\ 1, & x = a \end{cases}$$

10 Determine the points of discontinuity, of the function

$$\frac{x^2+5}{x^2+x+2}$$